

# Charmed Hadron Production in Polarized $pp$ Collisions

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# I. Introduction

## Proton Spin Puzzle

$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta g + \langle L \rangle_{q+g}$$

$\Delta\Sigma$  : Quark spin

$\Delta g$  : Gluon Spin

$\langle L \rangle_{q+g}$  : Orbital angular momentum of Quarks and Gluons

Experimental results :  $\Delta\Sigma \sim 0.3$

Naive quark model does not work!

Need more information about polarized partons  
in the proton!!

However!

The knowledge of the polarized gluon  
in the proton is still poor!

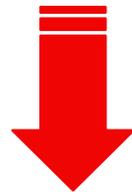
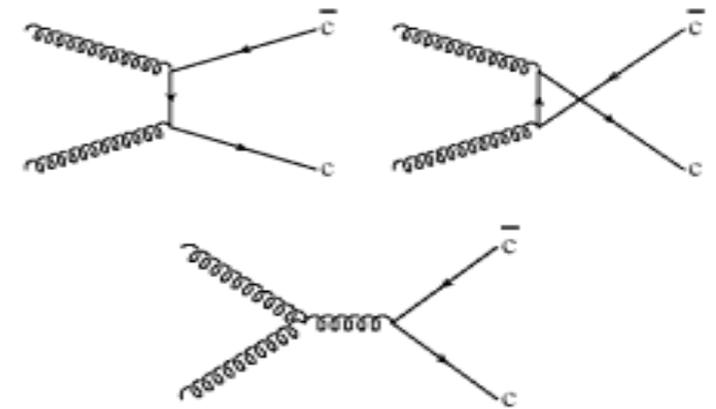
To extract the information about the polarized gluons, we propose such two processes:

$$\begin{aligned} \underline{\vec{P}} + P &\longrightarrow \underline{\vec{\Lambda}_c^+} + X, \\ \vec{P} + P &\longrightarrow \vec{D}^* + X. \end{aligned}$$

## Why Charmed Hadron Process?

$c$  quarks are not main constituents of the proton.

$c$  quark which is component of Charmed hadron is mainly produced via **gluon-gluon fusion**.

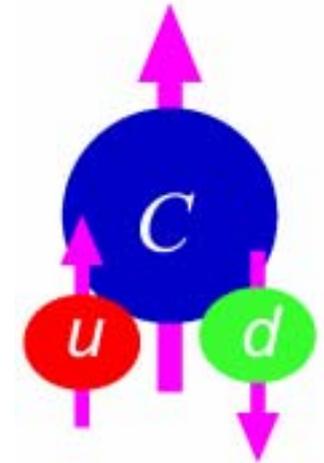


There is relation between the gluon spin and produced  $c$  quark spin.

*Especially*

$\Lambda_c^+$  is interesting !

Because!



$\Lambda_c^+$  baryon is composed of heavy  $c$  quark and antisymmetrically combined light  $u$  and  $d$  quarks.

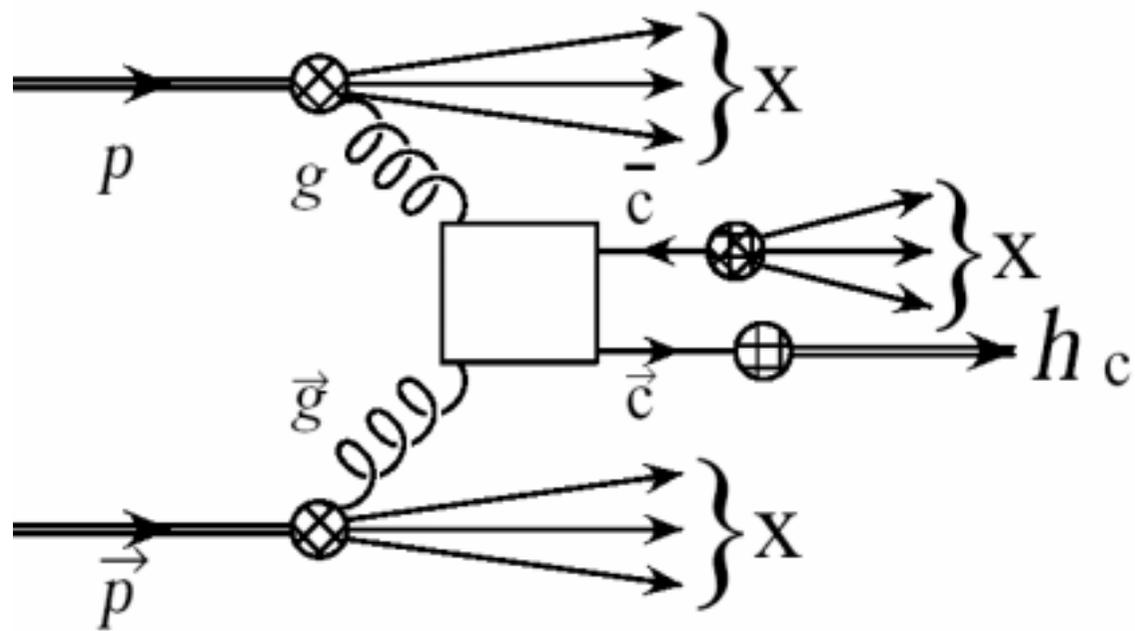
Spin of  $\Lambda_c^+$  baryon      Spin of  $c$  quark

Gluon in the initial proton is related produced  $c$  quark.

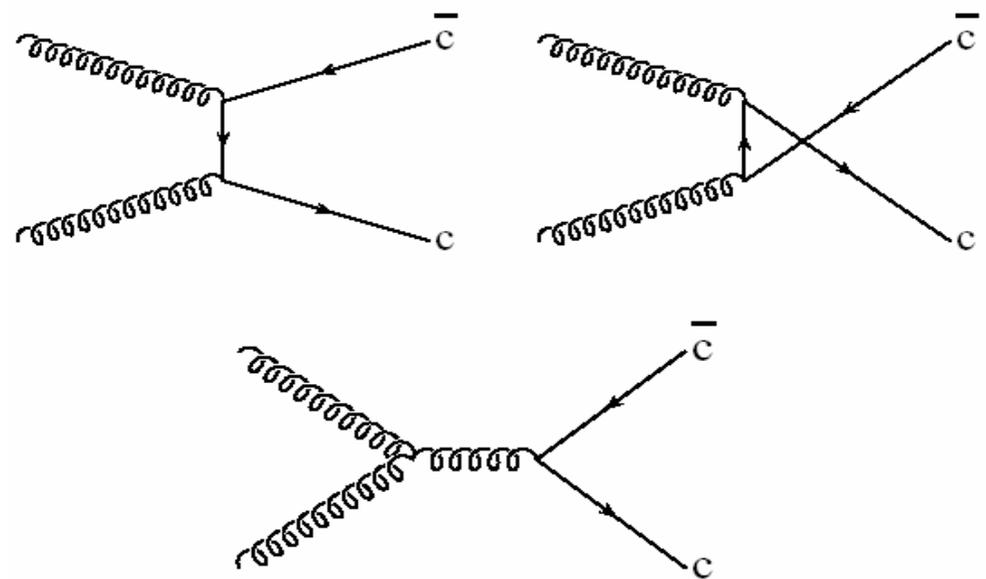
Observation of the spin of the produced  $\Lambda_c^+$  give us information about the polarized gluon in the proton

# II. Charmed Hadron production in $pp$ reaction

$$\vec{p} + p \rightarrow \vec{h}_c + X$$



Subprocesses



This process can be measured by RHIC experiment!!

To extract the information about polarized gluon distribution in the proton, we calculated two observables by using parton model.

## $p_T$ distribution

### 1. The spin correlation differential cross section

$$\frac{d\Delta\sigma}{dp_T} \equiv \frac{d\sigma(++)-d\sigma(+)-+)+d\sigma(---)-d\sigma(-+)}{dp_T}$$

$p_T$ : Transverse momentum of  $\Lambda_c^+$

$d\sigma(+, -)/dp_T$ : Spin dependent differential cross section

→ The positive helicity of the target proton

→ The negative helicity of the produced  $\Lambda_c^+$

### 2. The spin correlation asymmetry

$$A_{LL} \equiv \frac{d\sigma(++)-d\sigma(+)-+)+d\sigma(---)-d\sigma(-+)}{d\sigma(++)+d\sigma(+)-+)+d\sigma(---)+d\sigma(-+)} \frac{dp_T}{dp_T} = \frac{d\Delta\sigma/dp_T}{d\sigma/dp_T}$$

## $\eta$ distribution

### 1. The spin correlation differential cross section

$$\frac{d\Delta\sigma}{d\eta} \equiv \frac{d\sigma(++)-d\sigma(+-) + d\sigma(--)-d\sigma(-+)}{d\eta}$$

$\eta$  : Pseude-rapidity of  $\Lambda_c^+$

### 2. The spin correlation asymmetry

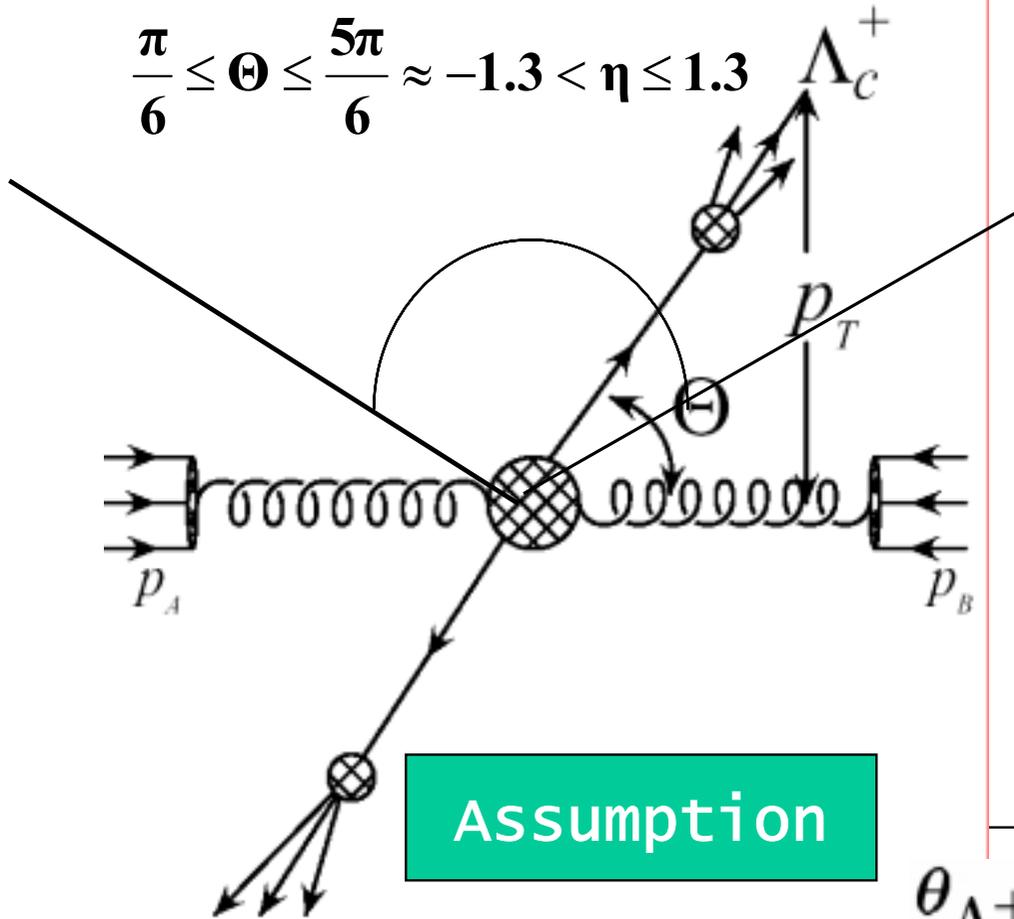
$$A_{LL} \equiv \frac{d\sigma(++)-d\sigma(+-) + d\sigma(--)-d\sigma(-+)/d\eta}{d\sigma(++)+d\sigma(+-) + d\sigma(--)+d\sigma(-+)/d\eta} = \frac{d\Delta\sigma/d\eta}{d\sigma/d\eta}$$

We will investigate

which distribution is the more optimal one ?

# Proton-proton center of mass frame

$$\frac{\pi}{6} \leq \Theta \leq \frac{5\pi}{6} \approx -1.3 < \eta \leq 1.3$$



$$p_{A/B} = \frac{\sqrt{s}}{2}(1, \pm\beta, \vec{0}) , \quad \beta \equiv \sqrt{1 - \frac{4m_p^2}{s}}$$

$$p_{\Lambda_c} = (E_{\Lambda_c}, p_L, p_T)$$

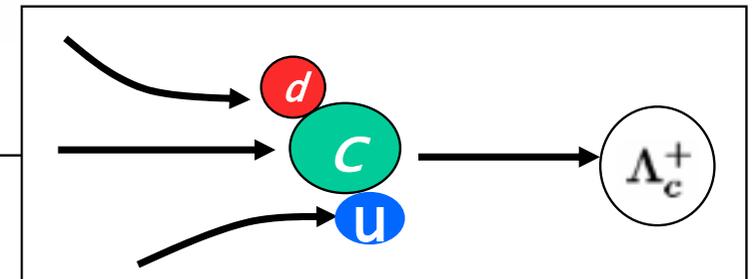
$$= (\sqrt{m_{\Lambda_c}^2 + (p_T \cosh \eta)^2}, p_T \sinh \eta, p_T)$$

$$p_{a,b} = x_{a,b} p_{A,B} , \quad p_c = \frac{p_{\Lambda_c}}{z}$$

$$\eta = -\ln \tan\left(\frac{\Theta}{2}\right)$$

Assumption

$$\theta_{\Lambda_c^+} \simeq \theta_c \equiv \Theta$$



$\theta_{\Lambda_c^+}$ : Scattering angle of the produced  $\Lambda_c^+$

$\theta_c$ : Scattering angle of the c quark in subprocess.

# The spin correlation differential cross section

## $P_T$ distribution

$$\frac{d\Delta\sigma}{dp_T} \equiv \int_{\eta^{\min}}^{\eta^{\max}} \int_{x_a^{\min}}^1 \int_{x_b^{\min}}^1 G_{g_a/p_A}(x_a, Q^2) \Delta G_{\vec{g}_b/\vec{p}_B}(x_b, Q^2) \\ \times \frac{d\Delta\hat{\sigma}}{d\hat{t}} \Delta D_{\vec{\Lambda}_c^+/\vec{c}}(z) \mathcal{J} d\Theta dx_a dx_b$$

$G_{g_a/p_A}(x_a, Q^2)$  : Unpolarized gluon distribution function

$\Delta G_{\vec{g}_b/\vec{p}_B}(x_b, Q^2)$  : Polarized gluon distribution function

$d\Delta\hat{\sigma}/d\hat{t}$  : Spin correlation differential cross section for subprocess

$\Delta D_{\vec{\Lambda}_c^+/\vec{c}}(z)$  : Spin dependent fragmentation function

$\mathcal{J}$  : Jacobian which transform the variables  $z$  and  $\hat{t}$  into  $\eta$  and  $p_T$

# III. Numerical Calculation

## Gluon Distribution Function of the Proton

Unpolarized Parton Distribution :  $G_{g_a/p_A}(x_a, Q^2)$

GRV 98

M. Glück, *et al.* Euro. Phys. J. C5(2000)461

Polarized Parton Distribution :  $\Delta G_{\vec{g}_b/\vec{p}_B}(x_b, Q^2)$

AAC

Y. Goto, *et al.* Phys.Rev.D62(2000)034017

GRSV 01

M. Glück *et al.* Phys.Rev.D63(2001)094005

These parameterization models are widely used.

# Fragmentations Function

Unpolarized fragmentation :  $D_{\Lambda_c^+/c}(z)$

Peterson Fragmentation Function

C. Peterson, *et al.* Phys. Rev. D27(1983)461

Unpolarized fragmentation :  $\Delta D_{\vec{\Lambda}_c^+/\vec{c}}(z)$

Unfortunately, we have at present no data about  $\Delta D_{\vec{\Lambda}_c^+/\vec{c}}(z)$



The analogy with the study of  $\Lambda$  polarization.

$$\Delta D_{\vec{\Lambda}_c^+/\vec{c}}(z) = C_{\Lambda_c^+/c}(z) D_{\Lambda_c^+/c}(z)$$

$C_{\Lambda_c^+/c}(z)$ : scale-independent spin transfer coefficient

$$\left\{ \begin{array}{ll} \text{Naïve non-rela. Quark model} & C_{\Lambda_c^+/c}(z) = 1 \\ \text{Jet fragmentation model} & C_{\Lambda_c^+/c}(z) = z \end{array} \right.$$

A. Bartl et al. Z. Phys. C6(1980)335

# Statistical sensitivity for $A_{LL}$

$$\delta A_{LL} \sim \frac{1}{P} \frac{1}{\sqrt{br_c \epsilon \mathcal{L} T \sigma}}$$

P : beam polarization = 70 %

Br<sub>c</sub> : Branching ratio Br(Λ<sub>c</sub><sup>+</sup> → pK<sup>-</sup>π<sup>+</sup>) ≈ 5%

E : The detecting efficiency = 10 %

L : Luminosity

$$L = 8 \times 10^{31} \text{ cm}^{-2} \text{ sec}^{-1} \text{ for } \sqrt{s} = 200 \text{ GeV}$$

$$L = 2 \times 10^{32} \text{ cm}^{-2} \text{ sec}^{-1} \text{ for } \sqrt{s} = 500 \text{ GeV}$$

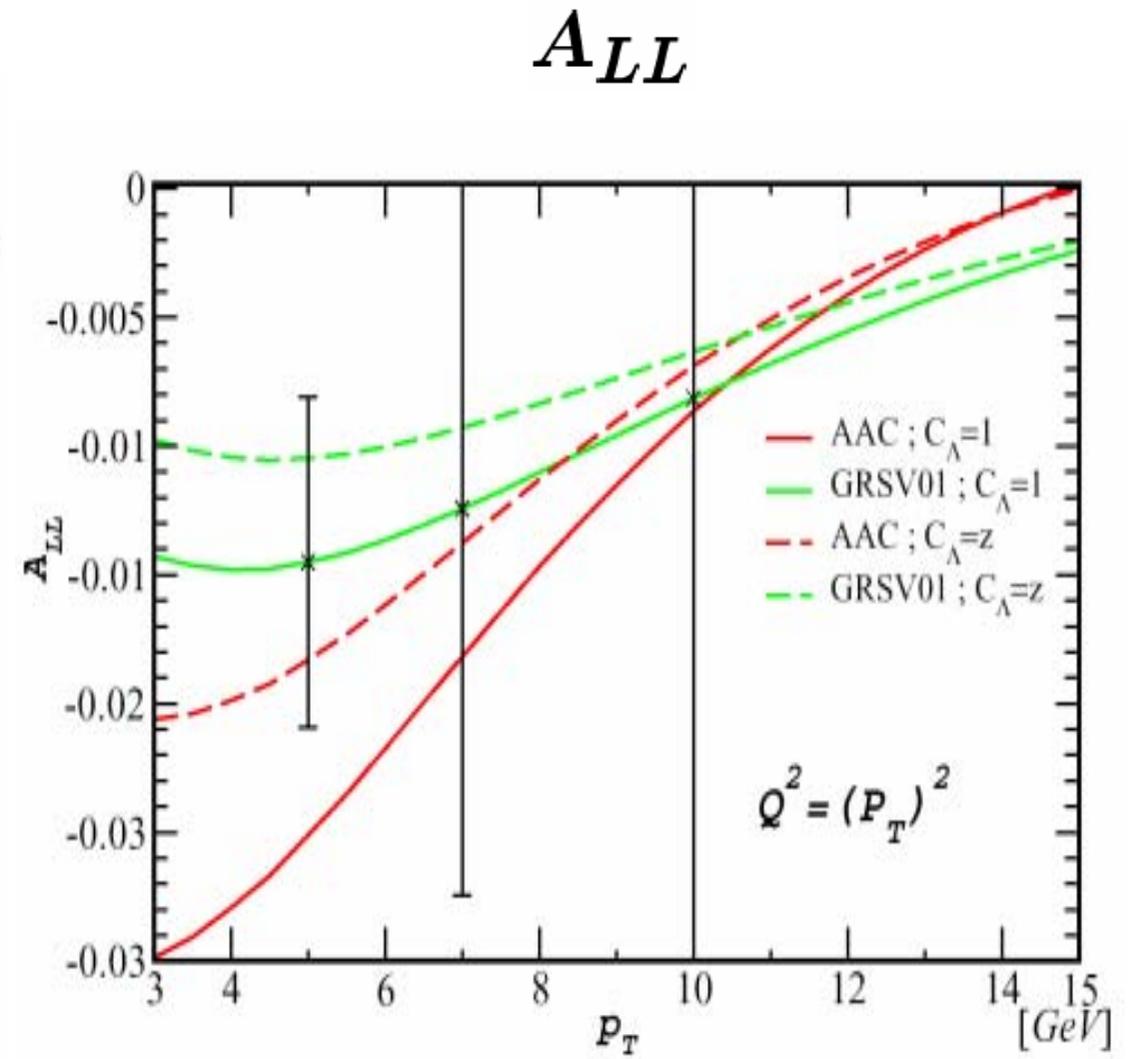
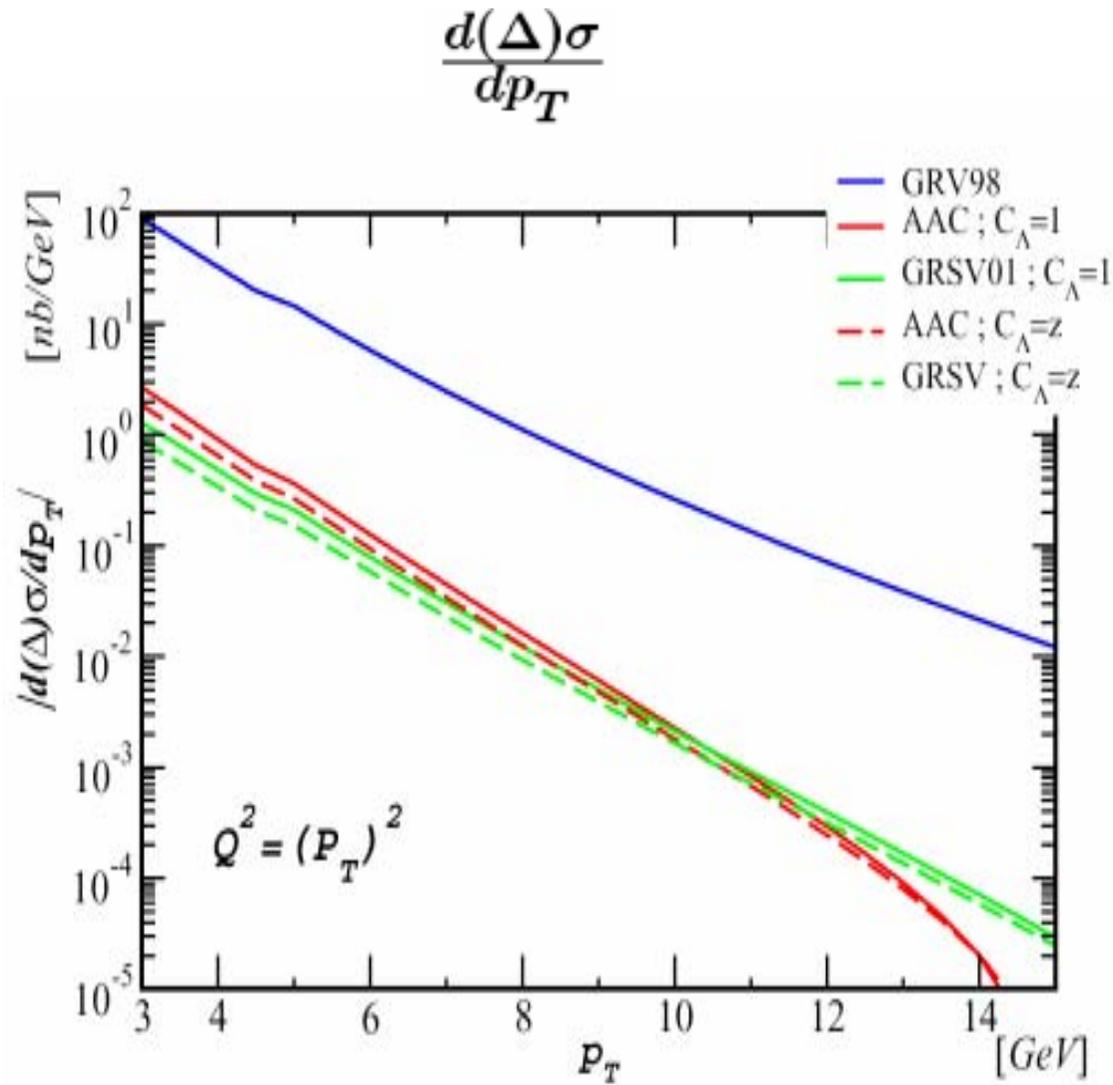
T : running time = 100-day

σ : unpolarized cross section integrated suitable  
 $p_T$  or  $\eta$  region.

$$\Delta p_T = 1 \text{ GeV} \quad \Delta \eta = 0.1$$

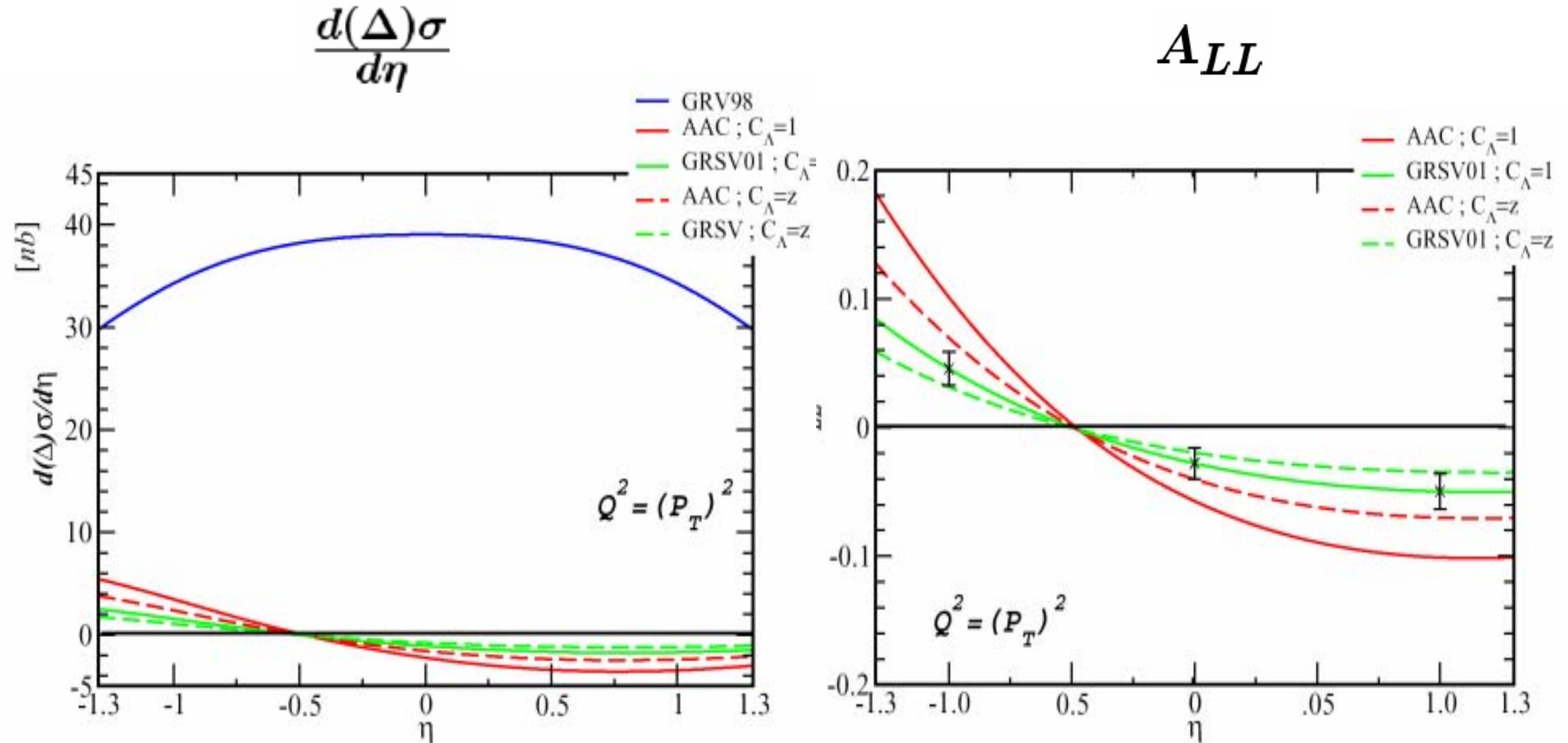
# $p_T$ distribution of $\frac{d(\Delta)\sigma}{dp_T}$ and $A_{LL}$ at $\sqrt{s} = 200\text{GeV}$

$$-1.3 \leq \eta \leq 1.3$$



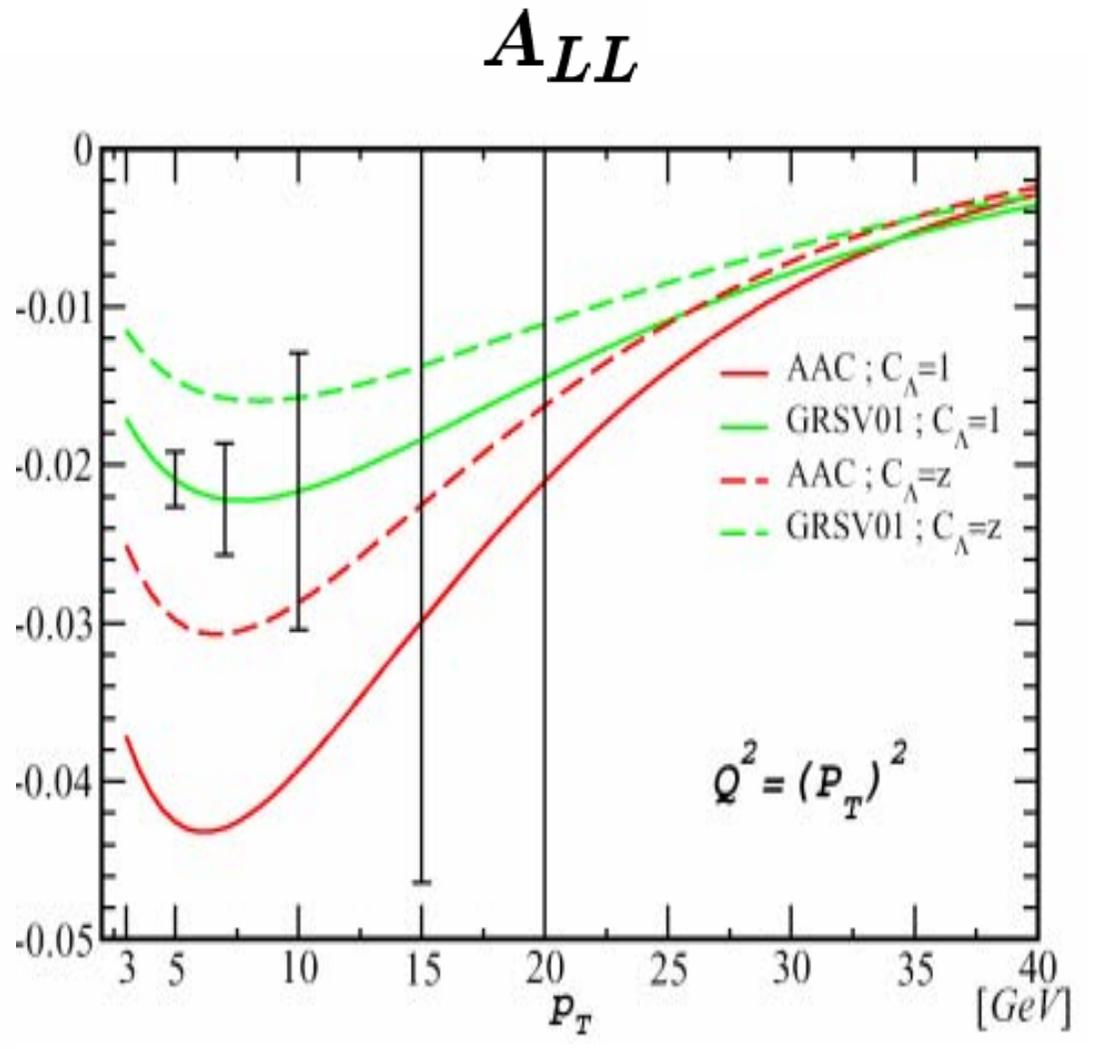
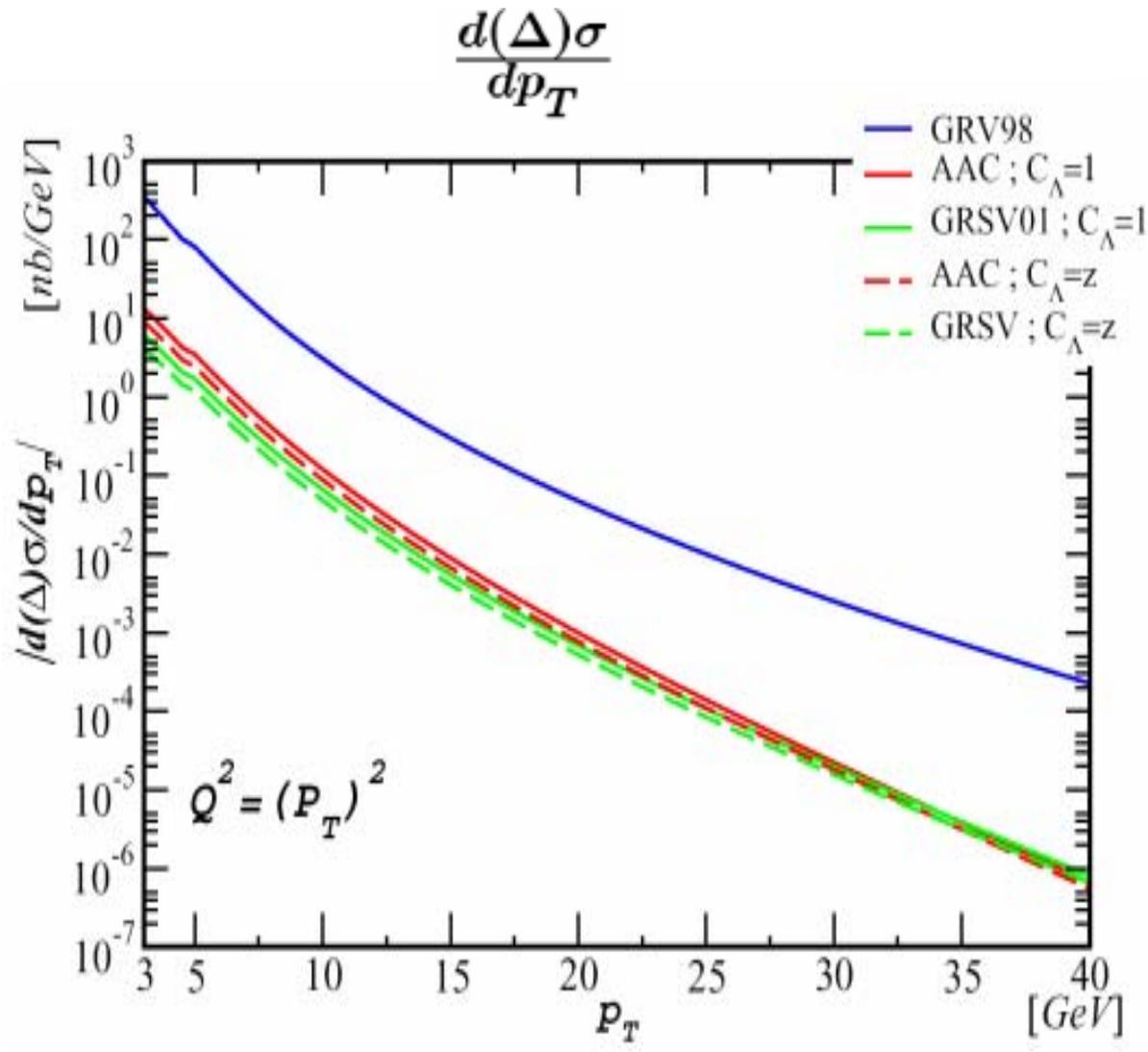
# $\eta$ distribution of $\frac{d(\Delta)\sigma}{d\eta}$ and $A_{LL}$ at $\sqrt{s} = 200\text{GeV}$

$$3 \leq p_T \leq 15$$



# $p_T$ distribution of $\frac{d(\Delta)\sigma}{dp_T}$ and $A_{LL}$ at $\sqrt{s} = 500\text{GeV}$

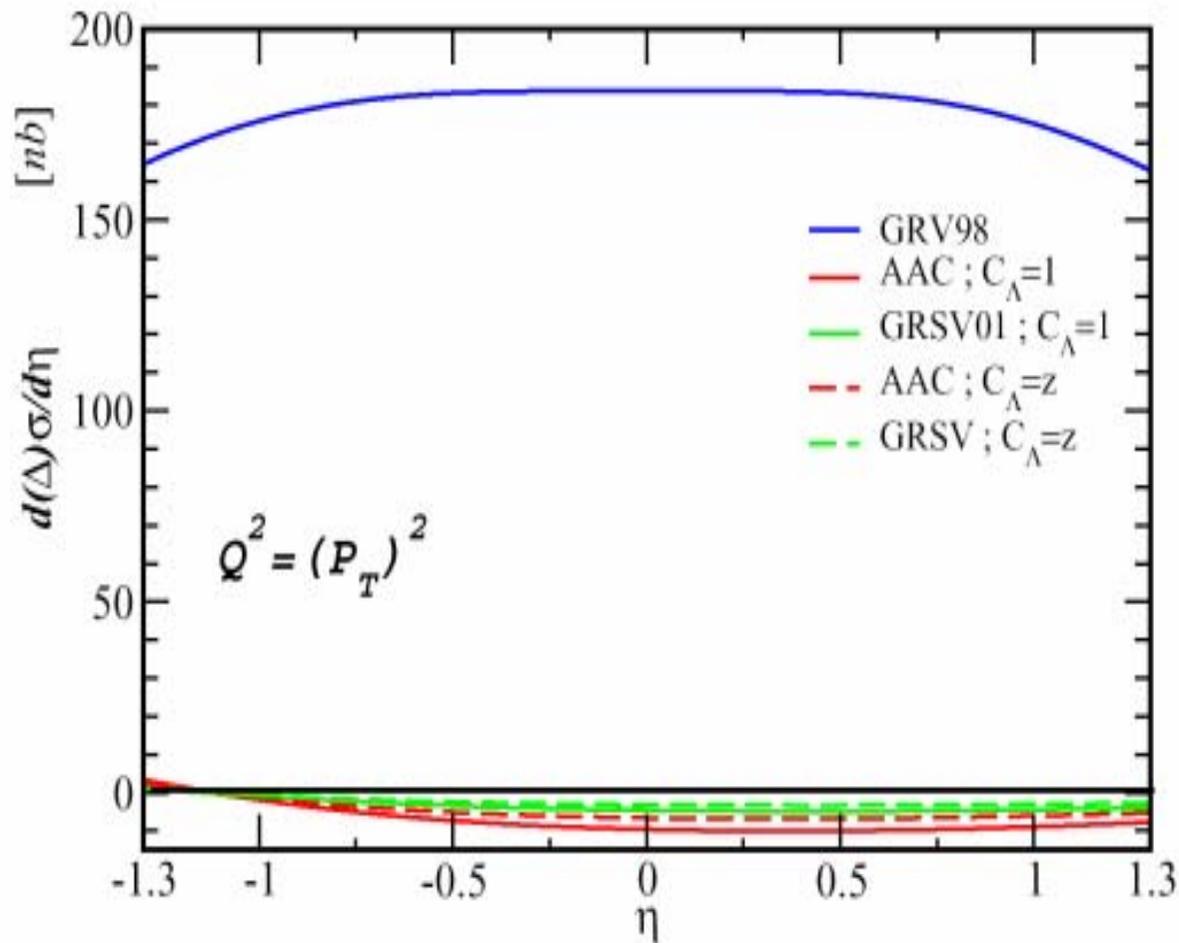
$$-1.3 \leq \eta \leq 1.3$$



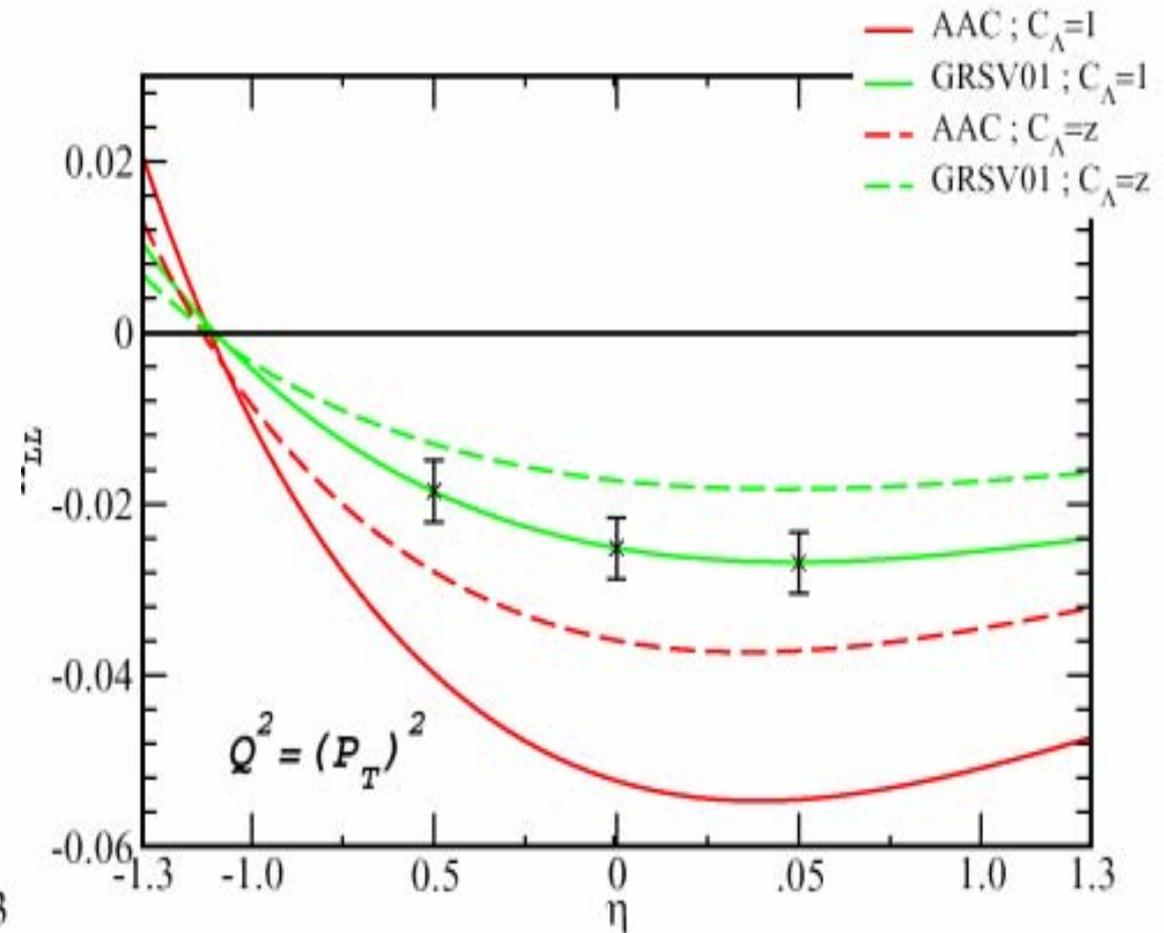
# $\eta$ distribution of $\frac{d(\Delta)\sigma}{d\eta}$ and $A_{LL}$ at $\sqrt{s} = 500\text{GeV}$

$$3 \leq p_T \leq 40$$

$$\frac{d(\Delta)\sigma}{d\eta}$$



$$A_{LL}$$



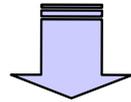
## IV. Summary (for $c$ production)

RHIC Experiment  
can measure this  
process.

For the process;  $\vec{P} + P \rightarrow \vec{\Lambda}_c^+ + X$ ,

The spin correlation diffractive cross section,  $\frac{d(\Delta)\sigma}{d\eta} / \frac{d(\Delta)\sigma}{dp_T}$  and spin asymmetry,  $A_{LL}$ , have been calculated for  $\sqrt{s} = 200\text{GeV}$  and  $\sqrt{s} = 500\text{GeV}$ .

The statistical sensitivity,  $\delta A_{LL}$  is estimated for RHIC experiment parameters.



$A_{LL}$  is sensitive to polarized gluon function.

$\eta$  distribution for  $A_{LL}$  is optimal observable.

$A_{LL}$  at  $\sqrt{s} = 200\text{GeV}$  is good observable for test of parameterization models for polarized gluon.

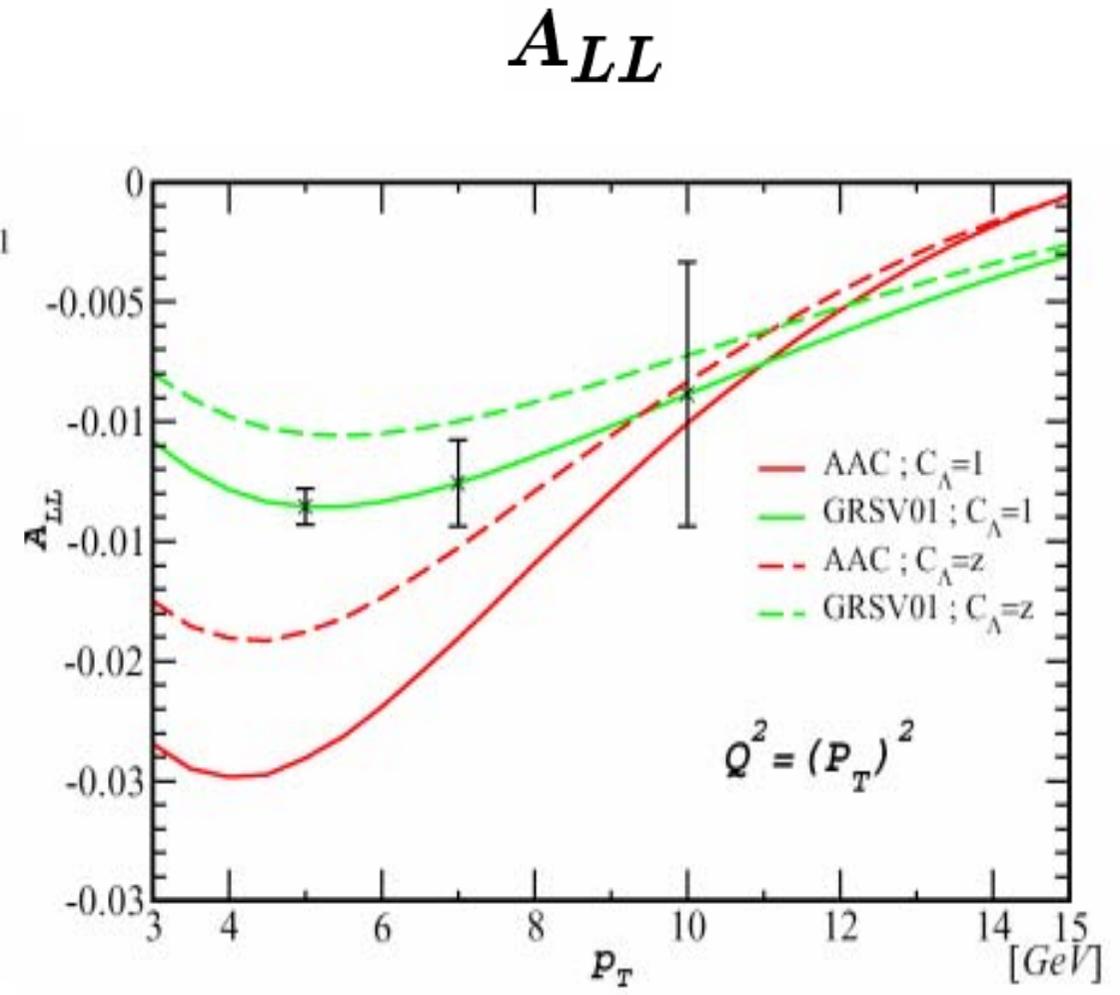
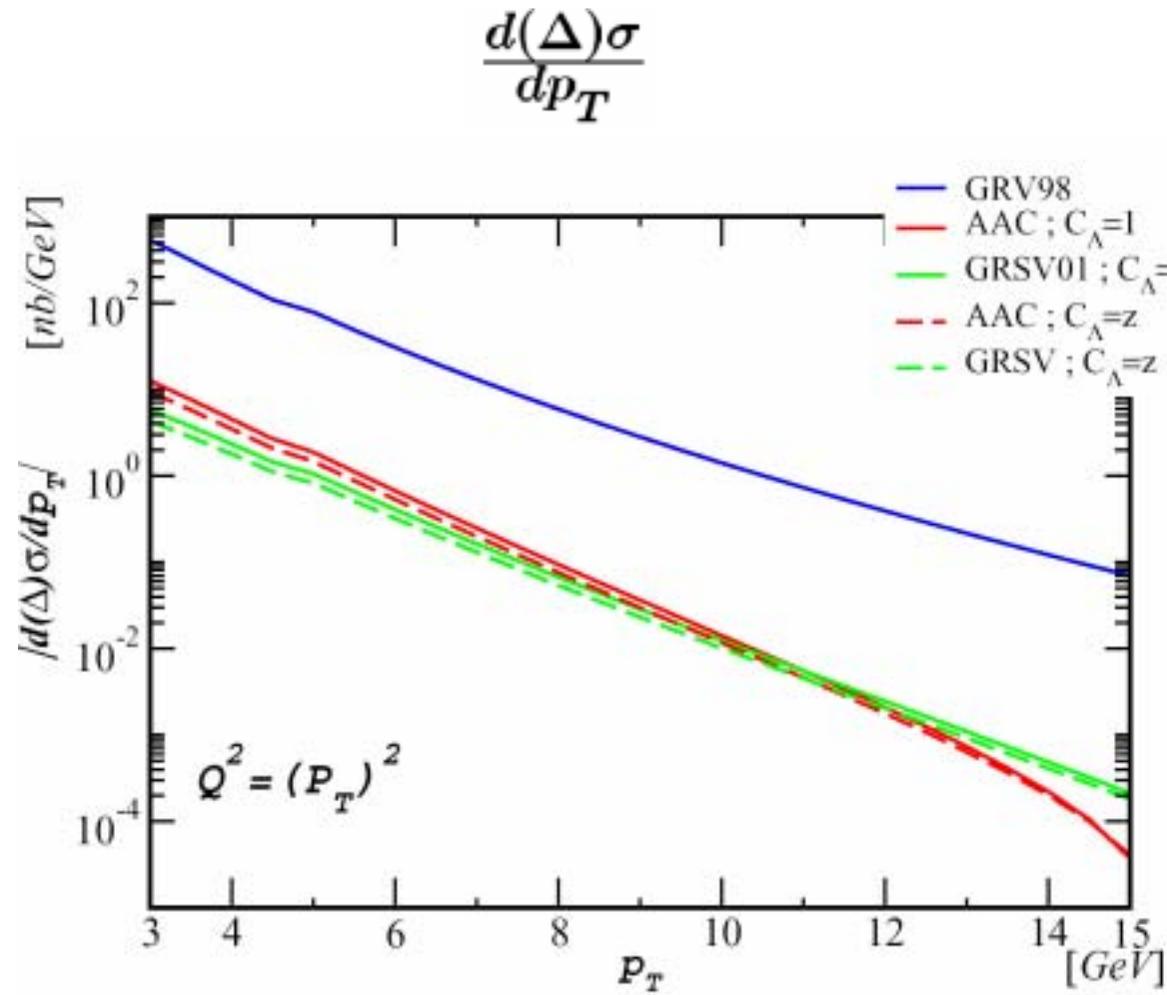
Study of polarized fragmentation function is important.

→  $D^*$  Process is also give us interesting information about polarized gluon in the proton.

**D\* meson production**

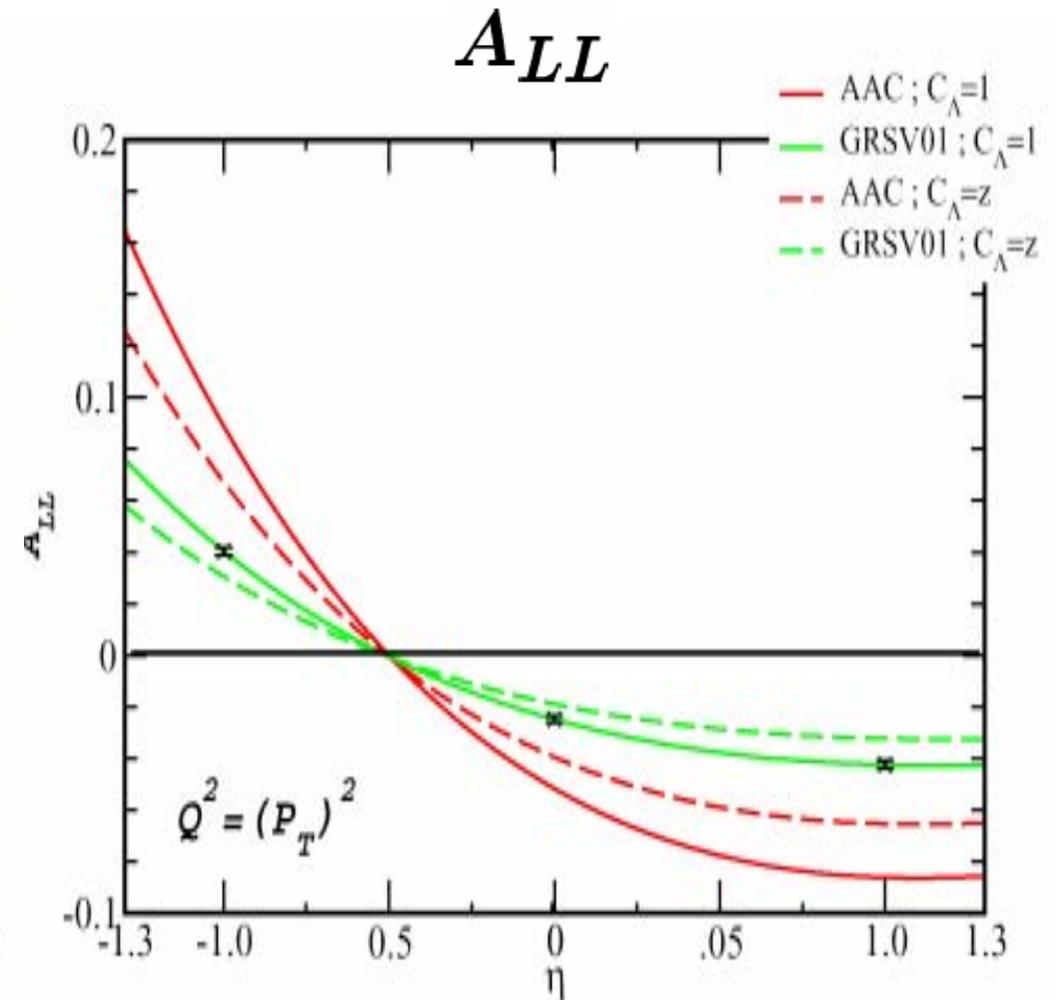
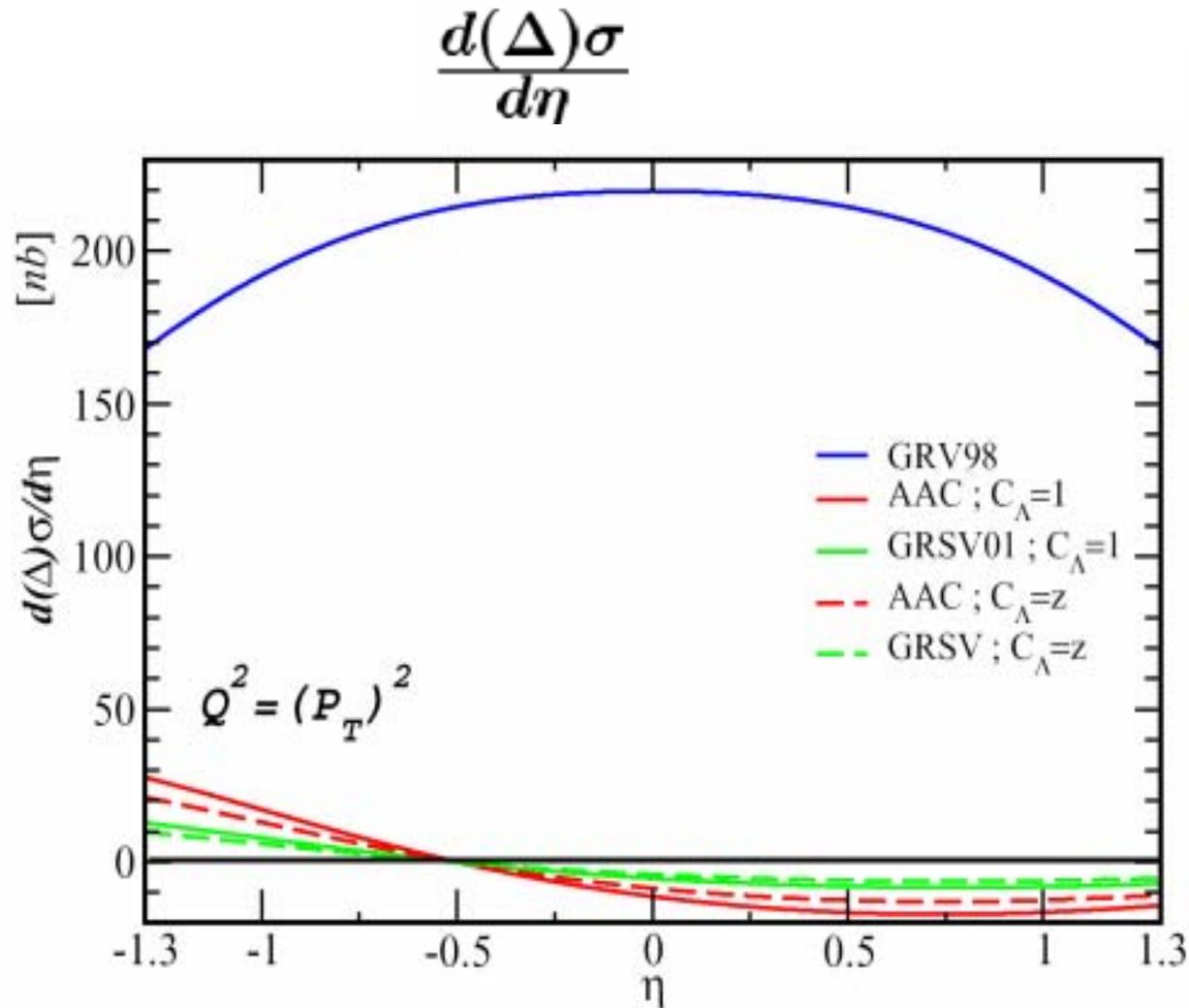
# $p_T$ distribution of $\frac{d(\Delta)\sigma}{dp_T}$ and $A_{LL}$ at $\sqrt{s} = 200\text{GeV}$

$$-1.3 \leq \eta \leq 1.3$$



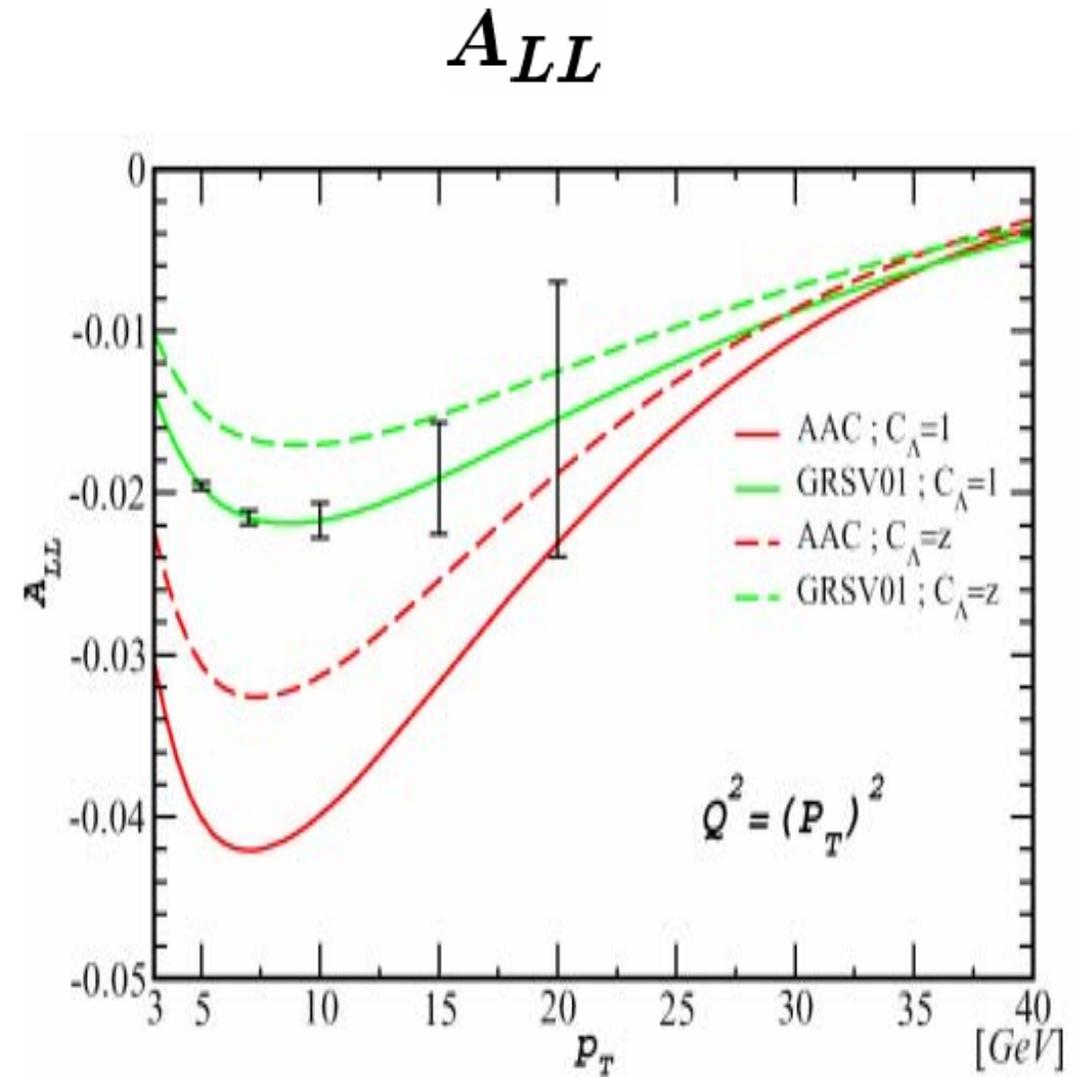
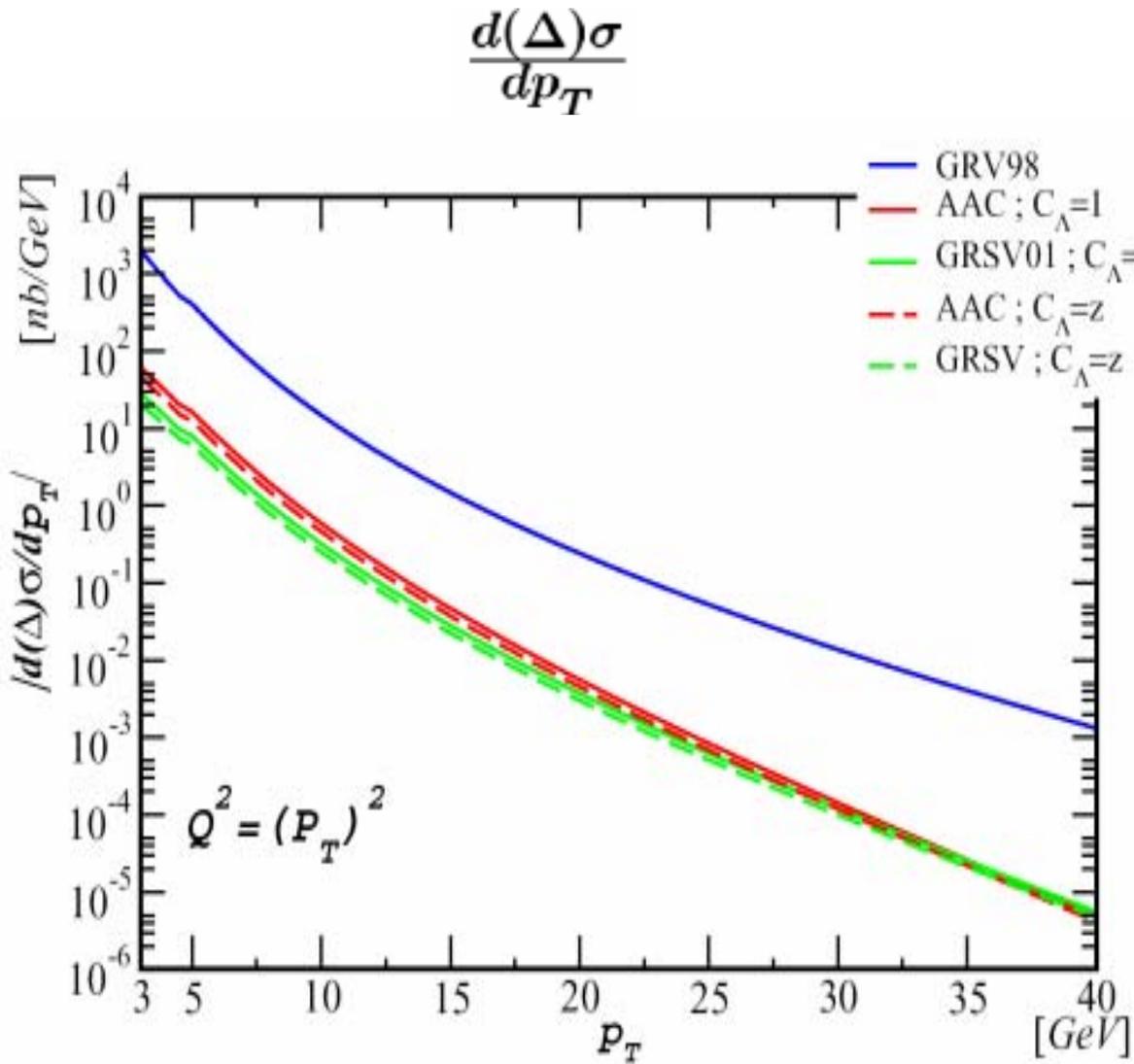
# $\eta$ distribution of $\frac{d(\Delta)\sigma}{d\eta}$ and $A_{LL}$ at $\sqrt{s} = 200\text{GeV}$

$$3 \leq p_T \leq 15$$



# $p_T$ distribution of $\frac{d(\Delta)\sigma}{dp_T}$ and $A_{LL}$ at $\sqrt{s} = 500\text{GeV}$

$$-1.3 \leq \eta \leq 1.3$$



# $\eta$ distribution of $\frac{d(\Delta)\sigma}{d\eta}$ and $A_{LL}$ at $\sqrt{s} = 500\text{GeV}$

$$3 \leq p_T \leq 40$$

